



SOLUTIONS

Joint Entrance Exam | IITJEE-2025

22nd JANUARY 2025 | Evening Shift

MATHEMATICS

SECTION – 1

$$1.(1) \quad (\lambda \bar{a} + 2\bar{b}) \cdot (3\bar{a} - \lambda \bar{b}) = 0 \Rightarrow 3\lambda - \frac{\lambda^2}{2} + 3 - 2\lambda = 0 \Rightarrow \frac{-\lambda^2}{2} + \lambda + 3 = 0 \Rightarrow \lambda^2 - 2\lambda - 6 = 0$$

$$2.(3) \quad \text{Case - I } f(A) = \{1\}$$

$$\text{Case - II } f(A) = \{1, 4/9/16\}$$

Select one out of 4/9/16 in

$${}^3C_1 \text{ way and assign 4 inputs among 2 outputs s.t. no output empty in } 2^4 - {}^2C_1 \cdot 1^4 = 14 \text{ ways}$$

$$\text{In } 2^4 - {}^2C_1 \cdot 1^4 = 14 \text{ ways} \quad \text{So, Case - II Total} = 14 \times {}^3C_1 = 42$$

$$\text{Case - III } f(A) = \{1, 4/9/16, 4/9/16\}$$

$$\left(3^4 - {}^3C_2 \cdot 2^4 + {}^3C_2 \cdot 1^4\right) \times {}^3C_2 = 108 \quad \text{Total} = 108 + 42 + 1 = 151$$

$$3.(3) \quad 2 \left[{}^5C_0 x^5 + {}^5C_2 x^3 (x^3 - 1) + {}^5C_4 x (x^3 - 1)^2 \right]$$

$$= 2 \left[x^5 + 10x^6 - 10x^3 + 5x^7 - 10x^4 + 5x \right]$$

$$\alpha = 10 \quad \beta = 2$$

$$x = -20 \quad s = 10$$

$$4.(3) \quad 2ae = 2 \cdot A \cdot (3e) = 2\sqrt{3}$$

$$\Rightarrow a = 3A$$

$$a - A = 2 \Rightarrow A = 1, a = 3$$

$$2ae = 2\sqrt{3} \Rightarrow ae = \sqrt{3}$$

$$b^2 = a^2 - a^2 e^2 = 6$$

$$L \cdot R_1 = 2 \times \frac{b^2}{a} = \frac{2 \times 6}{3} = 4$$

$$A(3e) = \sqrt{3} \quad B^2 = [A(3e)]^2 - A^2 = 2$$

$$L \cdot R_2 = \frac{2B^2}{A} = \frac{2 \times 2}{1} = 4$$

$$5.(1) \quad \text{Line PQ: } \frac{x+2}{3} = \frac{y+1}{2} = \frac{z-3}{2} = \lambda$$

$$Q \equiv (3\lambda - 2, 2\lambda - 1, 2\lambda + 3), R \equiv (1, 3, 3)$$

$$QR^2 = 25 \Rightarrow (3\lambda - 3)^2 + (2\lambda - 4)^2 + (2\lambda)^2 = 25 \Rightarrow 17\lambda^2 - 34\lambda = 0 \Rightarrow \lambda = 2$$

For Q

$$Q \equiv (4, 3, 7)$$

$$\overrightarrow{QP} = 6\hat{i} + 4\hat{j} + 4\hat{k}$$

$$\overrightarrow{QR} = 3\hat{i} + 0\hat{j} + 4\hat{k}$$

$$\overrightarrow{QP} \times \overrightarrow{QR} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 6 & 4 & 4 \\ 3 & 0 & 4 \end{vmatrix} = 16\hat{i} - 12\hat{j} - 12\hat{k}$$

$$(\text{Area})^2 = \frac{1}{4} \left| \overrightarrow{QP} \times \overrightarrow{QR} \right|^2 = \frac{1}{4} \times (256 + 144 + 144) = 136$$

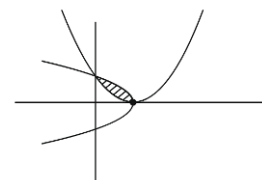
6.(3) Solve $(x^2 - 4x + 4)^2 = -8(x - 2)$

$$\Rightarrow (x - 2)(x - 2)^3 = -8(x - 2)$$

$$\Rightarrow x = 2 \text{ \& } (x - 2)^3 = -8 \Rightarrow x = 2 \text{ \& } x = 0$$

Point (2, 0) (0, 4)

$$\text{Area} = \int_0^2 [\sqrt{16 - 8x} - (x - 2)^2] dx$$



7.(4) $f'(x) = \frac{x^4 - 8x^2 + 15}{(+ve)} \cdot 2x = \frac{(x^2 - 3)(x^2 - 5) \cdot 2 \cdot x}{+ve} = \frac{(x - \sqrt{5})(x - \sqrt{3})(x)(x + \sqrt{3})(x + \sqrt{5})}{+ve}$

Minimum at $-\sqrt{5}, 0, \sqrt{5}$

Maximum at $-\sqrt{3}, \sqrt{3}$

8.(1) $\frac{k}{2}[2a + (k - 1)d] = 40 \quad \dots (i)$

$$\frac{k}{2}[2(a + d) + (k - 1)d] = 55 \quad \dots (ii)$$

$$(2k - 1)d = 27 \quad \dots (iii)$$

From (i) and (ii) Find kd , use in (iii) to get d .

9.(4) $12x^2 - 7x + 1 = 0$

Roots are $\frac{1}{4}, \frac{1}{3}$

$$\text{Let } P(A/B) = \frac{1}{4}$$

$$\Rightarrow \frac{P(A \cap B)}{P(B)} = \frac{1}{4} \Rightarrow P(B) = \frac{4}{10}$$

$$P(B/A) = \frac{1}{3} \Rightarrow P(A) = \frac{3}{10}$$

$$\frac{P(\overline{A \cap B})}{P(A \cup B)} = \frac{P(\overline{A \cap B})}{1 - P(A \cap B)} = \frac{1 - 0.1}{1 - \left[\frac{1}{3} + \frac{1}{4} - \frac{1}{10} \right]}$$

10.(4) $\alpha + \beta = -\frac{\cos \theta}{2}$

$$\alpha\beta = -\frac{1}{2}$$

$$\alpha^2 + \beta^2 = \frac{\cos^2 \theta}{4} + 1$$

$$\alpha^2 + \beta^4 = \left(\frac{\cos^2 \theta}{4} + 1 \right)^2 - 2 \times \frac{1}{4}$$

$$M = \left(\frac{1}{4} + 1 \right)^2 - \frac{1}{2}$$

$$m = (0 + 1)^2 - \frac{1}{2}$$

$$11.(3) \quad Q = (2\lambda + 1, -\lambda - 2, 2\lambda - 3)$$

$$P \equiv (2, -10, 1)$$

$$\overrightarrow{PQ} = (2\lambda - 1)\hat{i} + (-\lambda + 8)\hat{j} + (2\lambda - 4)\hat{k}$$

$$\overrightarrow{PQ} \cdot (2\hat{i} - \hat{j} + \hat{k}) = 0$$

$$\Rightarrow 2(2\lambda - 1) + (\lambda - 8) + 2(2\lambda - 4) = 0 \Rightarrow 9\lambda = 18 \Rightarrow \lambda = 2$$

$$\overrightarrow{PQ} = 3\hat{i} + 6\hat{j}; |\overrightarrow{PQ}| = \sqrt{45} = 3\sqrt{5}$$

$$12.(3) \quad z(1+i) + z(1-i) = 4 \Rightarrow x - y = 2$$

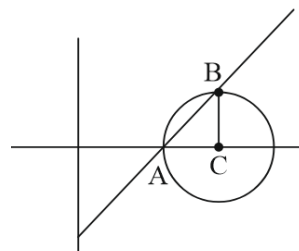
$$\text{Circle } (x-3)^2 + y^2 \leq 1$$

$$\text{Point of intersection } x = 2, 3$$

$$\beta = \text{area of sector } ACB - \text{area of } \triangle ACB$$

$$= \frac{\pi \times 1}{4} - \frac{1}{2} = \frac{\pi}{4} - \frac{1}{2}$$

$$\alpha = \pi - \beta; \alpha - \beta = -\lambda - 2\beta = \pi - 2\left(\frac{\pi}{4} - \frac{1}{2}\right) = \frac{\pi}{2} + 1$$



$$13.(3) \quad 48 = 4 \cdot a \cdot 4 \Rightarrow a = 3$$

$$S \equiv (3, 0)$$

$$P \equiv (4, 4, \sqrt{3}) \equiv (3t^2, 6t)$$

$$\Rightarrow 6t = 4\sqrt{3} \Rightarrow t = \frac{2\sqrt{3}}{3}$$

$$\text{For } -\frac{1}{t} = -\frac{3}{2\sqrt{3}} = -\frac{\sqrt{3}}{2}$$

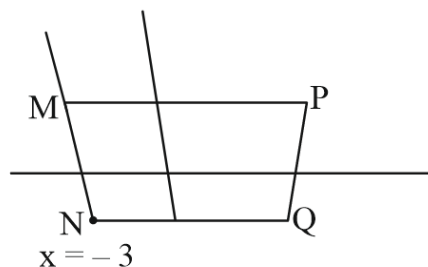
$$Q \equiv \left(3 \times \left(-\frac{\sqrt{3}}{2} \right)^2, 2 \times 3 \times \left(-\frac{\sqrt{3}}{2} \right) \right); Q \equiv \left(\frac{9}{4}, -3\sqrt{3} \right)$$

$$PM = 7$$

$$QN = 3 + \frac{9}{4} = \frac{21}{4}$$

$$MN = 7\sqrt{3}$$

$$\text{Area} = \frac{1}{2} \left(7 + \frac{21}{4} \right) \times 7\sqrt{3} = \frac{343\sqrt{3}}{8}$$



$$14.(4) \quad \boxed{G_1 G_2 G_3} \quad \boxed{B_1 B_2 B_3 B_4}$$

$$\text{Total} = 3! \times 4! \times 2!$$

$$B_1 B_2 \text{ together} : 2! \times 3! \times 3! \times 2!$$

$$3! \times 4! \times 2! - 2! \times 3! \times 3! \times 2!$$

$$= 3! \times 2! [4! - 3! \times 2!] = 6 \times 2 \times [24 - 12] = 12 \times 12 = 144$$

$$15.(1) \quad \Delta = \begin{vmatrix} 1 & 1 & 2 \\ 2 & 3 & a \\ -1 & -3 & b \end{vmatrix} = 0$$

$$\Delta_3 = \begin{vmatrix} 1 & 1 & 6 \\ 2 & 3 & a+1 \\ -1 & -3 & 2b \end{vmatrix} = 0$$

16.(3) $\text{adj}(\text{adj}A) = |A|^{n-2} A$

$$B = \text{adj}(\text{adj}2A) = |2A|^1 (2A) = 2^3 |A| 2A$$

$$\Rightarrow B = 8A$$

$$\text{Trace}(B) = 8 (\text{trace } A)$$

$$= 24$$

$$|B| = 8^3 |A| = 256.$$

17.(3) $2 \sin^2 \theta = 1 - 2 \sin^2 \theta$

$$\Rightarrow \sin^2 \theta = \frac{1}{4}$$

$$2 - 2 \sin^2 \theta = 3 \sin \theta$$

$$\Rightarrow 2 \sin^2 \theta + 3 \sin \theta - 2 = 0$$

$$\Rightarrow 2 \sin^2 \theta + 4 \sin \theta - \sin \theta - 2 = 0$$

$$\Rightarrow \sin \theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{6}, \frac{5\pi}{6}$$

18.(4) $\int e^x [f(x) + f'(x)] dx$

$$f(x) = \frac{x \sin^{-1} x}{\sqrt{1-x^2}} = e^x f(x) + C$$

$$g(x) = e^x \cdot \frac{x \cdot \sin^{-1} x}{\sqrt{1-x^2}} + C$$

$$g\left(\frac{1}{2}\right) = \sqrt{e} \frac{1 \times 2}{2\sqrt{3}} \times \frac{\pi}{6}$$

19.(3) $\lim_{x \rightarrow \infty} e^{[f(x)-1]} \cdot g(x)$

$$\lim_{x \rightarrow \infty} e^{\left[\left(\frac{e}{1-e}\right)\left[\frac{1}{e} - \frac{x}{1+x}\right] - 1\right]} \cdot x$$

$$x = \frac{1}{h}$$

$$\lim_{h \rightarrow 0} e^{\left[\left(\frac{e}{1-e}\right)\left(\frac{1}{e} - \frac{1}{1+h}\right) - 1\right]} \frac{1}{h}$$

$$\lim_{h \rightarrow 0} e^{\left[\left(\frac{e}{1-e}\right)\left[\frac{1+h-e}{e(e+h)}\right] - 1\right]} \frac{1}{h}$$

$$\lim_{h \rightarrow 0} e^{\left[\frac{e+eh-e^2-e(1-e)(1+h)}{(1-e) \cdot e \cdot (1+h)}\right]} \frac{1}{h}$$

$$\Rightarrow \alpha = e^{\frac{e}{1-e}}$$

$$\log \alpha = \frac{e}{1-e}$$

$$20.(2) \left(2e^{\tan^{-1} y} - x \right) \frac{dy}{dx} = 1 + y^2$$

$$\Rightarrow \frac{2e^{\tan^{-1} y} - x}{1 + y^2} = \frac{dx}{dy} \Rightarrow \frac{dx}{dy} + \frac{1}{1 + y^2} \cdot x = \frac{2e^{\tan^{-1} y}}{1 + y^2}$$

$$I.F. = e^{\tan^{-1} y}$$

$$\text{equation } x \cdot e^{\tan^{-1} y} = \int \frac{e^{\tan^{-1} y} \cdot 2 \cdot e^{\tan^{-1} y}}{1 + y^2} dy$$

$$\text{Let } e^{\tan^{-1} y} = u \Rightarrow \frac{e^{\tan^{-1} y}}{1 + y^2} dy = du$$

$$= 2 \int u du \Rightarrow x \cdot e^{\tan^{-1} y} = e^{2 \tan^{-1} y} + C ; \quad y = 0, x = 1 \Rightarrow c = 0 \quad \text{Now put } y = \frac{1}{\sqrt{3}}$$

SECTION – 2

$$21.(465) r \cdot r \frac{{}^{30}C_r \cdot {}^{30}C_r}{{}^{30}C_{r-1}} = r \cdot r {}^{30}C_r : \left(\frac{30 - r + 1}{r} \right)$$

$$= r \cdot {}^{30}C_r \cdot (31 - r) = 31r \cdot {}^{30}C_r - r^2 \cdot {}^{30}C_r$$

$$S = 31 \cdot \sum_{r=1}^{30} r \cdot {}^{30}C_r - \sum_{r=1}^{30} r^2 \cdot {}^{30}C_r$$

$$= 31 \cdot 30 \cdot 2^{29} - 30 \cdot 31 \cdot 2^{28} = 2^{29} (31 \cdot 30 - 15 \cdot 31) = 2^{29} (15 \times 31) = 465 \times 2^{29}$$

$$22.(145) 6 + 10 \cos \alpha - 10 \sin \alpha = a \quad \dots(i)$$

$$8 + 10 \cos \alpha - 10 \sin \alpha = g \quad \dots(ii)$$

$$\Rightarrow 10 \cos \alpha - 10 \sin \alpha = 1 \quad \dots(iii)$$

$$\Rightarrow 100 \sin 2\alpha = 99 \quad \dots(iv)$$

from (iii)

$$(i) \Rightarrow a = 7$$

$$\text{Now } \frac{8 + 10 \cos \alpha - 10 \sin \alpha}{3} = k$$

$$\Rightarrow \frac{8 + 1}{3} = k \Rightarrow k = 3 \text{ and } \frac{6 + 10 \cos \alpha - 10 \sin \alpha}{3} = h$$

$$\Rightarrow 3h = 7 \quad \text{Ans. } 5 \times 7 - 7 + 6 \times 3 + 99 = 145$$

$$23.(28) \sin \theta = \frac{1}{x} \Rightarrow \cos \theta = \sqrt{1 - \frac{1}{x^2}}$$

$$\sin(60 - \theta) = \frac{4}{x}$$

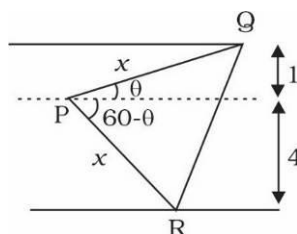
$$\Rightarrow \frac{\sqrt{3}}{2} \cdot \sqrt{1 - \frac{1}{x^2}} - \frac{1}{x} \cdot \frac{1}{2} = \frac{4}{x}$$

$$\Rightarrow \frac{\sqrt{3}}{2} \sqrt{1 - \frac{1}{x^2}} = \frac{9}{2x}$$

$$\Rightarrow 3 \left(1 - \frac{1}{x^2} \right) = \frac{81}{x^2}$$

$$\Rightarrow 1 - \frac{1}{x^2} = \frac{27}{x^2} \Rightarrow \frac{28}{x^2} = 1$$

$$\Rightarrow x^2 = 28$$



24.(3) Some question in NCERT (1, 3) must be present

Need to decide for (2, 1), (3, 2), (3, 1)

One possible relation

$\{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3), (1, 3)\}$

2nd possible add (2, 1) only

3rd possible add (3, 2) only

if we add (3, 1), for transitivity all other have to be added.

25.(27) I.F. = $e^{\frac{1}{2} \int \frac{2x dx}{x^2-1}} = e^{\frac{1}{2} \log|1-x^2|} = \sqrt{1-x^2}$

solution $y \cdot (\sqrt{1-x^2}) = \int (x^6 + 4x) dx$

$$\Rightarrow y\sqrt{1-x^2} = \frac{x^7}{7} + 2x^2 + 0$$

$$f(x) = \frac{x^7}{7\sqrt{1-x^2}} + \frac{2x^2}{\sqrt{1-x^2}}$$

$$\int_{-1/2}^{1/2} \frac{x^7}{7\sqrt{1-x^2}} dx = 0$$

$$\int_{-1/2}^{1/2} \frac{2x^2}{\sqrt{1-x^2}} dx = 4 \int_0^{1/2} \frac{x^2}{\sqrt{1-x^2}} dx$$

$$= 4 \left[\int_0^{1/2} \frac{1-(1-x^2)}{\sqrt{1-x^2}} dx \right] = 4 \left[\int_0^{1/2} \frac{dx}{\sqrt{1-x^2}} - \int_0^{1/2} \sqrt{1-x^2} dx \right]$$

$$4 \left[\sin^{-1} x \Big|_0^{1/2} - \left\{ \frac{x}{2} \sqrt{1-x^2} + \frac{1}{2} \sin^{-1} x \right\} \Big|_0^{1/2} \right] = \frac{\pi}{3} - \frac{\sqrt{3}}{2}$$

PHYSICS

SECTION – 1

26.(4) $\vec{F} = 2\hat{i} + \hat{j} + 2\hat{k}$

$$\vec{r} = \hat{i} + \hat{j} + \hat{k}$$

$$\vec{\tau} = \vec{r} \times \vec{F} = \hat{i}(1) - \hat{j}(0) + \hat{k}(-1) = \hat{i} - \hat{k}$$

27.(4) $\frac{hc}{\lambda} = 1 + 2 = 3$

$$\frac{hc}{\lambda} = 6eV$$

$$6eV = \phi + KE_{\max}$$

$$KE_{\max} = 5eV$$

28.(4) $\beta = \frac{\lambda D}{d}$

$$\lambda_{\text{Red}} > \lambda_{\text{violet}} \quad \therefore \quad \beta_{\text{Red}} > \beta_{\text{violet}} \quad \therefore \quad \text{Assertion is false}$$

29.(1) $evB = \frac{mw^2}{R}$

$$mwR = \frac{2h}{2\pi}$$

$$eB = \frac{m}{R} \cdot \frac{2h}{2\pi mR}$$

$$R^2 = \frac{h}{\pi eB}$$

$$R = \left(\frac{h}{\pi eB} \right)^{1/2}$$

30.(2) $V_B = 0$

$$E_A = \frac{2kp}{r^3} = E_0$$

$$E_B = \frac{-kp}{(2r)^3} = \frac{-Kp}{8r^3}$$

$$E_B = \frac{E_0}{16}$$

31.(3) Energy = $\frac{1}{2} CV^2$

$$\text{Force} \times \text{displacement} = C \cdot (\text{Electric field} \times d)^2$$

$$\text{Force} \times \text{displacement} = C \cdot \left(\frac{\text{Force} \times d}{\text{Charge}} \right)^2$$

$$C = (\text{charge})^2 \cdot \frac{\text{displacement}}{\text{Force} \times d^2}$$

$$C = \frac{(\text{Charge})^2}{\text{Force} \times d}$$

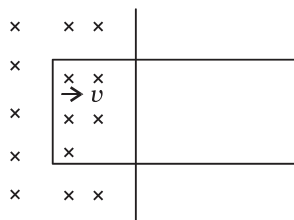
$$[F] = [C^2 M^{-1} L^{-2} T^2]$$

32.(1) $\text{Density} = \frac{\text{mass}}{\text{volume}}$

$$\frac{\Delta d}{d} \times 100 = \left(\frac{\Delta m}{m} + \frac{2\Delta r}{r} + \frac{\Delta l}{l} \right) \times 100 = \left(\frac{.003}{.6} + \frac{2 \times .01}{.5} + \frac{.05}{10} \right) \times 100 = 0.5 + 4 + 0.5 = 5\%$$

33.(1) No option is matching

34.(2)



$$\epsilon_1 = Blv = \text{Constant}$$

35.(3) Work done = 0

$$\vec{F} \cdot \vec{S} = 0$$

$$2(1) + b(-2) + 1(-1) = 0$$

$$2 - 2b - 1 = 0$$

$$1 = 2b$$

$$b = \frac{1}{2}$$

36.(1) Theoretical

37.(2) $K_A + 0 = K_B + mg(2 - 2\cos 30^\circ)$

$$K_A + 0 = K_C + mg(2 + 2\cos 60^\circ)$$

$$K_B = \frac{1}{2}m(100) - m(10)(2 - 13)$$

$$K_C = \frac{1}{2}m(100) - m(10)(3)$$

$$\frac{K_B}{K_C} = \frac{50 - 10(2 - \sqrt{3})}{50 - 30} = \frac{3 + \sqrt{3}}{2}$$

38.(1) $\gamma_1 = \frac{7}{5} = 1.4, \gamma_2 = \frac{9}{7} = 1.28$

39.(2) $g_p = \frac{G \cdot 4M}{4R^2} = g_E ; T = 2\pi\sqrt{\frac{l}{g}}$

Both are correct but not correct explanation

40.(4) $A_1V_1 = A_2V_2$

$$4 \times 2 = 1 \times V_2$$

$$V_2 = 8$$

41.(3) $2\mu t = \lambda$ {For maximum transmission}

$$2 \times 2 \times t = 550 \text{ nm}$$

$$t = \frac{550}{4} = 137.5 \text{ nm}$$

42.(4) $P = \frac{1}{f} = (\mu - 1) \left(\frac{1}{R} + \frac{1}{R} \right) = (\mu - 1) \left(\frac{2}{R} \right) = 4D$

$$P' = \frac{1}{f'} = (\mu - 1) \left(\frac{1}{R} - \frac{1}{\infty} \right) = \frac{\mu - 1}{R} = 2D$$

$$43.(2) \quad I_0 = \frac{V_0}{Z} = \frac{V_0}{R}$$

$$I' = \frac{V_0}{Z} = \frac{V_0}{2R} = \frac{I_0}{2}$$

$$44.(4) \quad (KE)_i = \frac{1}{2}(0.1)(20)^2 = 20J$$

$$(KE)_f = \frac{1}{2}(0.1)(10)^2 = 5J$$

$$\Delta KE = 15J$$

$$45.(3) \quad mg = B_F + F_V$$

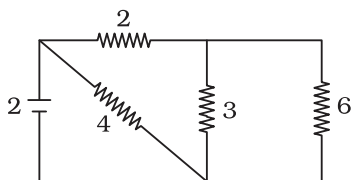
$$F_V = mg - B_F = mg - \frac{mg}{2} = \frac{mg}{2}$$

SECTION - 2

$$46.(1200) \quad i_{\text{displacement for total area}} = i_{\text{conduction}}$$

$$\text{But for small area is } = \epsilon_0 \times \frac{d}{dt}(EA) = \epsilon_0(3.2) \frac{d}{dt} \left(\frac{Q}{A_{\text{total}} \epsilon_0} \right) = 3.2 \times \frac{6}{16} = 2 \times \frac{6}{10} A = 1200 \text{ mA}$$

47.(1) Right side circuit is short



$$\therefore i_0 = 1A$$

$$48.(1) \quad B_{\text{net}} = \frac{\mu_0(4)}{2\pi(0.4)} - \frac{\mu_0(5)}{2\pi(1)} = 2 \times 10^{-7} \times 100 - 2 \times 10^{-7} \times 50 = 2 \times 10^{-7} (50) = 10^{-5} T$$

$$49.(1) \quad 1m \rightarrow 2M$$

$$dx \rightarrow 2Mdx$$

$$\int (dp)A = \int (2Mdx)w^2x$$

$$PA = 2Mw^2 \frac{x^2}{2} \Big|_0^1$$

$$PA = Mw^2 1^2$$

$$w = \left(\frac{F}{M} \right)^{1/2}$$

$$50.(2) \quad R = \frac{mv}{qB}$$

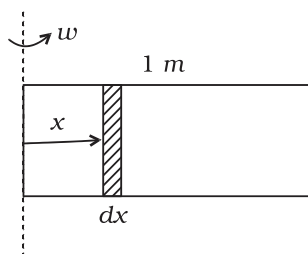
$$qB = \frac{mv}{R}$$

$$qvB = qE$$

$$\frac{mv^2}{R} = qE$$

$$\frac{1.6 \times 10^{-27} \times 4 \times 10^{10}}{2 \times 10^{-2}} = 1.6 \times 10^{-19} \times E$$

$$E = 2 \times 10^{-8} \times 10^{12} = 2 \times 10^4$$

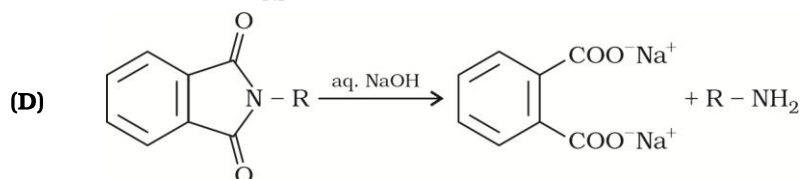
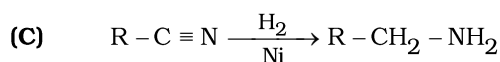
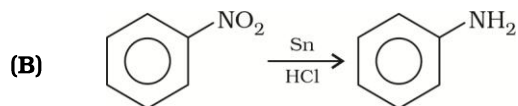
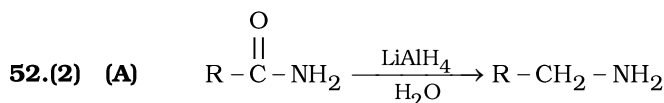


CHEMISTRY

SECTION – 1

51.(3) Extreme left : Group-1 elements form basic oxides.

Extreme right : Group-17 elements form acids with their oxides on reaction with water.

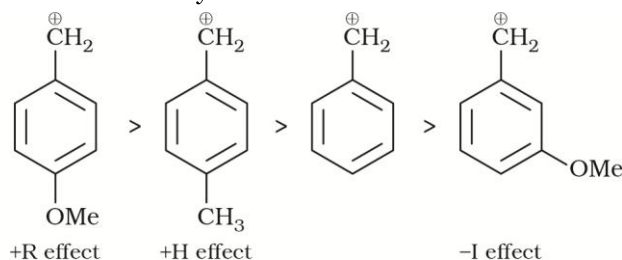


53.(1) Refer NCERT : Electrochemistry [Section-2.8, Corrosion]

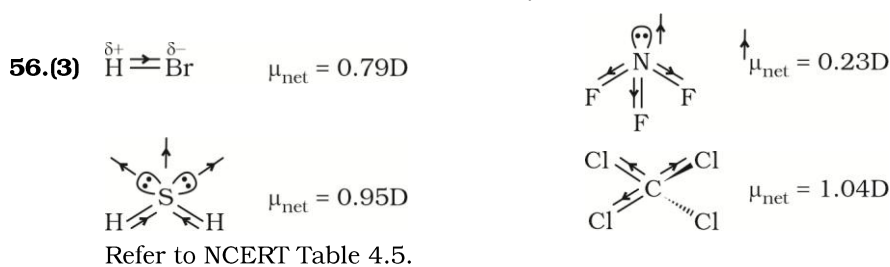
During corrosion, pure metal acts as an anode and impure metal act as a cathode.

The rate of corrosion is more in acidic medium than in alkaline medium.

54.(4) Order of stability of carbocations:

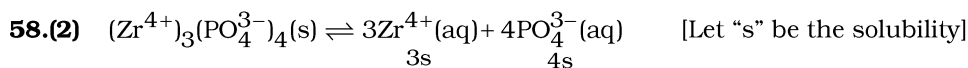


55.(4) $2p_x$ and $2p_y$ are degenerate orbitals and hence they have equal energy levels. There would be no spectral line observed for $2p_x \rightarrow 2p_y$ transition.

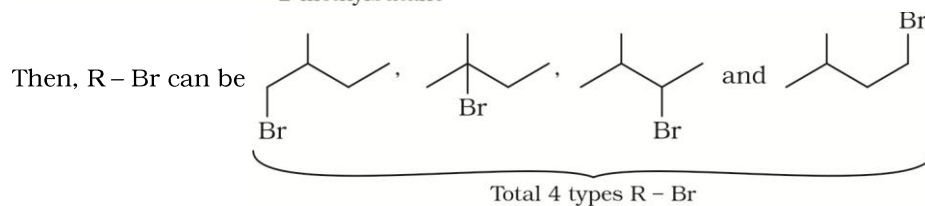
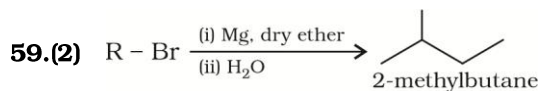


57.(1) $\left(\frac{\partial H}{\partial T}\right)_P = C_P$ and $\left(\frac{\partial U}{\partial T}\right)_V = C_V$ $\therefore dG = VdP - SdT$

Hence, $\left(\frac{\partial G}{\partial T}\right)_P = -S$ and $\left(\frac{\partial G}{\partial P}\right)_T = V$



$$K_{\text{sp}} = (3s)^3 \cdot (4s)^4 \Rightarrow K_{\text{sp}} = 6912s^7 \Rightarrow s = \left(\frac{K_{\text{sp}}}{6912}\right)^{1/7}$$



60.(1) The single $N-N$ bond is weaker than the single $P-P$ bond because of high interelectronic repulsion of the non-bonding electrons, owing to the small bond length.

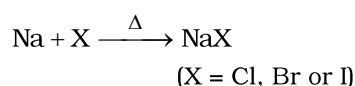
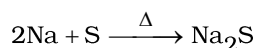
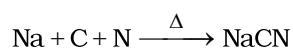
Hence, N has maximum covalency = 4.

61.(3) **Standard fisher projection** : Highest oxidised carbon is at the top. Here it is $-CHO$.

We compare position of $-OH$ group at last chiral carbon in the standard fisher projection with D-glyceraldehyde for a D-Configuration.

Options A, B and D are correlated with D-glyceraldehyde.

62.(4) For Lassaigne's test, sodium is used and not magnesium to convert covalent into ionic form.



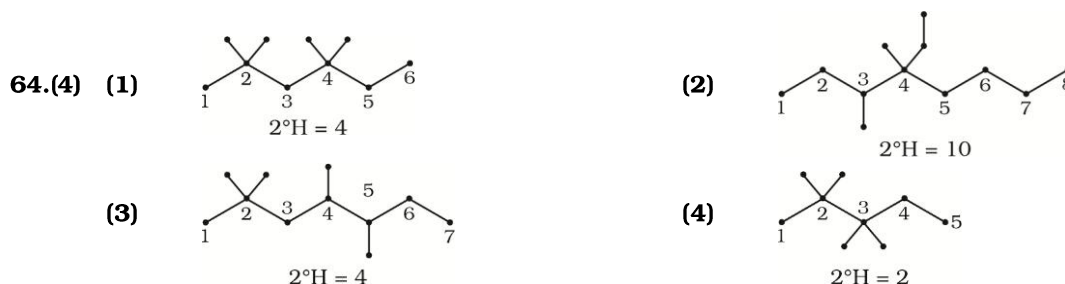
C, N, S and X come from organic compound.

Cyanide, sulphide and halide of sodium so formed on sodium fusion are extracted from the fused mass by boiling it with distilled water. This extract is known as sodium fusion extract.

63.(1) Except $[Fe(CN)_5NO]^{2-}$, all are homoleptic as have only one type of ligand.

High spin complexes : $[CoF_6]^{3-}$, $[Cr(H_2O)_6]^{2+}$

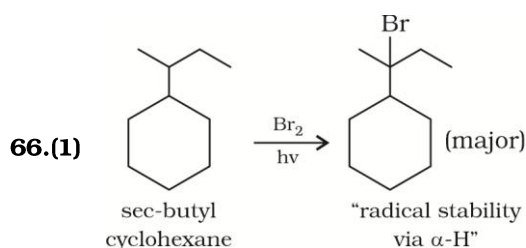
Low spin complexes : $[Fe(CN)_6]^{4-}$, $[Co(NH_3)_6]^{3+}$

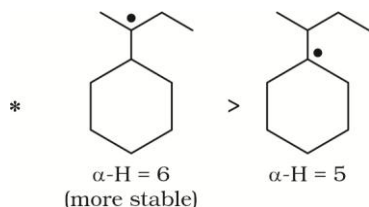


65.(4) $d_{NaCl} = 1.25 \text{ g/mL}$; $M_{NaCl} = 3 \text{ M}$

$$\text{Molality, } m = \frac{M \times 1000}{1000d - MM_0}$$

$$\Rightarrow m = \frac{1000 \times 3}{(1000 \times 1.25) - (3 \times 58.5)} = \frac{3000}{1074.5} = 2.79 \text{ molal}$$





67.(1) The species having Cl-atom in its maximum oxidation state (+7) or minimum oxidation state (-1) will not undergo disproportionation reaction.

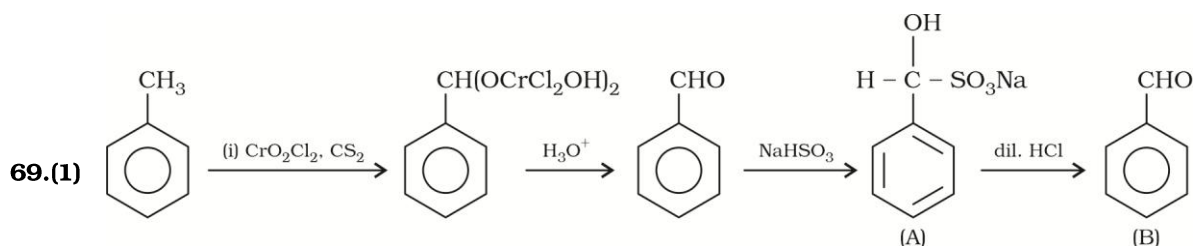
ClO_4^- : Cl has +7 oxidation state; ClO^- : Cl has +1 oxidation state

ClO_3^- : Cl has +5 oxidation state; ClO_2^- : Cl has +3 oxidation state

68.(1) Activation energy for forward reaction = $E_1 + E_2$

Activation energy for backward reaction = E_1

Product has more energy than reactant.



70.(1) $\text{CFSE} \propto \text{Type of field } [\Delta_t < \Delta_0]$

$\text{CFSE} \propto \text{Strength of ligand}$

$\text{CFSE} \propto \text{Charge on central metal ion}$

* en is a chelating as well as more stronger ligand than NH_3 .

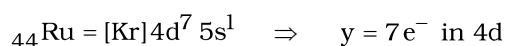
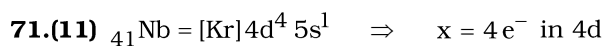
$\therefore [\text{Co}(\text{NH}_3)_6]^{3+} < [\text{Co}(\text{en})_3]^{3+}$: CFSE order

* Due to higher charge on central metal ion.

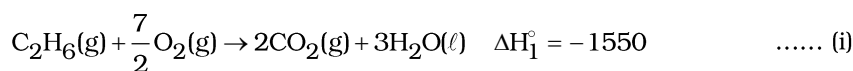
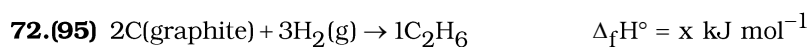
$\therefore [\text{Co}(\text{NH}_3)_6]^{2+} < [\text{Co}(\text{NH}_3)_6]^{3+}$: CFSE order

* Due to type of field ($\Delta_0 > \Delta_t$)

$\therefore [\text{Co}(\text{NH}_3)_4]^{2+} < [\text{Co}(\text{NH}_3)_6]^{2+}$: CFSE order

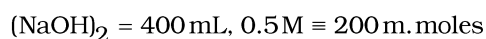
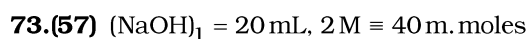
SECTION – 2

$x + y = 11$

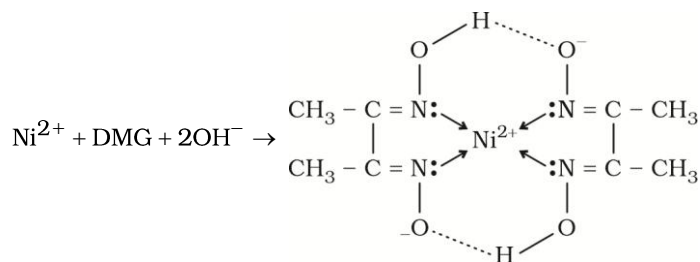
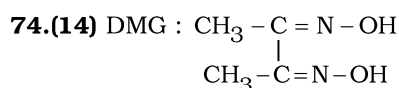


On solving, $2 \times (ii) + 3 \times (iii) - (i)$, we get,

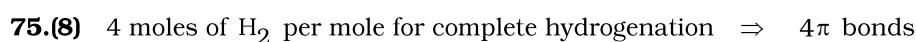
$\Delta_f H^\circ_{\text{C}_2\text{H}_6} = 2 \times (-393.5) + 3 \times (-286) - (-1550) = -787 - 858 + 1550 = -95 \text{ kJ mol}^{-1}$



Final NaOH conc. = $\frac{(200 + 40)}{420 \text{ mL}} \text{ m.moles} = \frac{240}{420} \text{ M} = 0.571 \text{ M} = 57.1 \times 10^{-2} \text{ M}$



Number of H-atoms in the complex = 14



* C_6H_6 is a symmetrical dialkyne.

